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### First-Principles calculations at the atomic scale

- Electronic Structure
- Atomic forces and stresses
- Molecular Dynamics





The "ultimate model" for electrons in a material

$$H = \sum_{i} \left[ -\frac{\hbar^2 \Delta_i}{2m_e} + \sum_{l} \frac{-e^2}{4\pi\epsilon_0} \frac{Z_l}{|\mathbf{r}_i - \mathbf{R}_l|} ; \right] + \frac{1}{2} \sum_{i \neq j} \frac{e^2}{4\pi\epsilon_0} \frac{1}{|\mathbf{r}_i - \mathbf{r}_j|}$$

 $\hat{H}\Psi = E\Psi \qquad \Psi(\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_n)$ We could compute "everything"



Density-functional theory  $E = E[n] \quad n(\mathbf{r})$  $\{-\nabla^2 + V_{\text{eff}}[n](\mathbf{r})\}\psi_i = \varepsilon_i\psi_i$  One electron  $V_{\text{eff}}[n](\mathbf{r}) = V_{\text{ext}}(\mathbf{r}) + V_{\text{H}}[n](\mathbf{r}) + V_{\text{xc}}[n](\mathbf{r})$ 



#### The SIESTA method for ab-initio materials simulation

Soler, Artacho, García, Gale, Junquera, Ordejón, Sánchez-Portal J. Phys. Cond. Matt (2002)

> HOMO and LUMO of DNA (800 atoms, small computer) Linear-scaling calculation (1999)





#### More than 3600 citations

More than 1000 active users



Localized atomic orbitals

Cu phthalocyanine on Ag(001) 1400 atoms



#### TranSIESTA: Electronic transport

Brandbyge, Mozos, Ordejón, Taylor and Stokbro Phys. Rev. B. (2002) --- 900 citations



## **OBJECTIVES**

- Optimization of the SIESTA code
- Performance of a "Grand-Challenge" calculation



$$\psi_i(r) = \sum_{\mu} \phi_{\mu}(r) c_{\mu i}, \qquad \stackrel{s}{\sim} \stackrel{a_3}{\sim} \stackrel{a_4}{\sim} \stackrel{ree atom}{} \stackrel{This work}{\sim} \stackrel{sanley}{\sim} d \qquad \stackrel{a_4}{\sim} \stackrel{a_4}{\sim} \stackrel{a_4}{\sim} \stackrel{a_5}{\sim} \stackrel{a_4}{\sim} \stackrel{a_4}{\sim} \stackrel{a_5}{\sim} \stackrel{a_4}{\sim} \stackrel{a_4}{\sim} \stackrel{a_5}{\sim} \stackrel{a_4}{\sim} \stackrel{a_4}{\sim} \stackrel{a_5}{\sim} \stackrel{a_4}{\sim} \stackrel{a_5}{\sim} \stackrel{a_4}{\sim} \stackrel{a_4}{\sim} \stackrel{a_5}{\sim} \stackrel{a_5}{\sim} \stackrel{a_4}{\sim} \stackrel{a_5}{\sim} \stackrel{a_5}{\sim} \stackrel{a_4}{\sim} \stackrel{a_4}{\sim} \stackrel{a_5}{\sim} \stackrel{a_4}{\sim} \stackrel{a_4}{\sim} \stackrel{a_5}{\sim} \stackrel{a_5}{\sim} \stackrel{a_4}{\sim} \stackrel{a_6}{\sim} \stackrel{a_$$

$$H^{\alpha\beta}_{\mu\nu} = \langle \phi_{\mu} | \hat{T} + \hat{V}^{KB} + V^{NA}(r) + \delta V^{H}(r) + V^{\alpha\beta}_{XC}(r) | \phi_{\nu} \rangle$$
  
Hamiltonian

$$S_{\mu\nu} = \langle \phi_{\mu} | \phi_{\nu} \rangle$$

$$\sum_{\nu\beta} (H^{\alpha\beta}_{\mu\nu} - E_i S_{\mu\nu} \delta^{\alpha\beta}) c^{\beta}_{\nu i} = 0$$

Output 
$$\begin{cases}
\rho(\mathbf{r}) = \sum_{\mu\nu} \rho_{\mu\nu} \phi_{\nu}^{*}(\mathbf{r}) \phi_{\mu}(\mathbf{r}) \\
E^{BS} = \sum_{i} n_{i} \langle \psi_{i} | \hat{H} | \psi_{i} \rangle = \sum_{\mu\nu} H_{\mu\nu} \rho_{\nu\mu} = \operatorname{Tr}(H\rho) \\
\rho_{\mu\nu} = \sum_{i} c_{\mu i} n_{i} c_{i\nu} \quad \text{Density matrix}
\end{cases}$$

## **S**parsity

S





 $\rho_{\mu\nu}$  is not strictly sparse but only a sparse subset is needed



# (Finite-range basis orbitals)

0.3

0.1 **(a)** 

(i)) ∧ Free atom

This work Sankey

#### • TASK 8.1: "Optimization of the SIESTA code"

- Massive parallelization for optimal performance in computers with thousands of processors (allowing the treatment of systems with many thousands of atoms)
- -Operation in MPI (present) and OpenMP (future) modes.

$$H^{\alpha\beta}_{\mu\nu} = \langle \phi_{\mu} | \hat{T} + \hat{V}^{KB} + V^{NA}(r) + \delta V^{H}(r) + V^{\alpha\beta}_{XC}(r) | \phi_{\nu} \rangle$$
  
Hamiltonian Improvement of load-balancing

of real-space mesh operations



$$\sum_{\nu\beta} (H^{\alpha\beta}_{\mu\nu} - E_i S_{\mu\nu} \delta^{\alpha\beta}) c^{\beta}_{\nu i} = 0$$
 Generalized  
eigenvalue problem







#### (Rogeli Grima, J.M. Cela, BSC)



P2

P5

P3



Optimization of the diagonalization: Ideas to beat ScaLapack

ScaLapack: Uses dense matrices; limited scalability

- Use an iterative method, exploiting the sparse character of the H and S matrices.
  - Krylov-type methods: Not appropriate when the number of eigenvectors to compute is relatively large.
- Split-spectrum methods for trivial parallelization at the top level.



## Sugiura-Sakurai and FEAST algorithms

(Implementation and benchmarking: Georg Huhs, BSC)







### Alternative electronic-structure method Pole Expansion plus Selected Inversion

$$f_{\beta}(\epsilon_i - \mu) = \frac{2}{1 + e^{\beta(\epsilon_i - \mu)}}$$

 $\hat{\rho} = f_{\beta}(\hat{H} - \mu)$ 







$$f_{\beta}(\epsilon_i - \mu) \approx Im \sum_{l=1}^{P} \frac{\omega_l}{\epsilon_i - (z_l + \mu)}$$

$$\hat{\rho} = Im\left(\sum_{l=1}^{P} \frac{\omega_l}{H - (z_l + \mu)S}\right)$$



$$\hat{\rho} = Im\left(\sum_{l=1}^{P} \frac{\omega_l}{H - (z_l + \mu)S}\right)$$

One inversion per pole

Only a limited number of elements needed in density matrix



#### **Selected Inversion**

$$A = \begin{pmatrix} a & b^{T} \\ b & \hat{A} \end{pmatrix}$$
$$(A =)LDL^{T} = \begin{pmatrix} 1 & \\ l & \hat{L} \end{pmatrix} \begin{pmatrix} \alpha & \\ & \hat{A} - bb^{T}/\alpha \end{pmatrix} \begin{pmatrix} 1 & l^{T} \\ & \hat{L} \end{pmatrix}$$
$$A^{-1} = \begin{pmatrix} \alpha^{-1} + l^{T}S^{-1}l & -l^{T}S^{-1} \\ & -S^{-1}l & S^{-1} \end{pmatrix}$$



### Pole Expansion plus Selected Inversion (Lin Lin, Chao Yang, LBNL)

Trivially parallel over poles, with perfect load balancing

For sufficiently big problems (quasi-)1D:  $\mathcal{O}(N)$ (quasi-)2D:  $\mathcal{O}(N^{3/2})$ 3D:  $\mathcal{O}(N^2)$ 

(Due to sparsity of the target density matrix)

Will beat Scalapack for large systems: It can use thousands of cores efficiently, with small memory footprint.

There is still scope for further optimization of the factorization and inversion operations



### Pole Expansion plus Selected Inversion (PEXSI)

Implementation of interface to SIESTA and benchmarking: Alberto García (ICMAB) and Georg Huhs (BSC)

Development of heuristics to handle the variation of the chemical potential during the self-consistent-field updates

Main test systems: quasi-2D C-BN structures





# O(N) functional



Optimization of sparse-matrix operation (CASE) Easier case: Minimization without localization (CASE, F. Corsetti)



# • TASK 8.2: "Tools for data handling and implementation of new simulation techniques"

- New library to process operational parameters in parallel (Raúl de la Cruz, BSC)
- Use of more efficient formats for data storage (HDF5, ongoing)
- Implementation of a mechanism to dispatch tasks in parallel, used to drive SIESTA from a Path-Integral program.



Quantum effects described by Path-Integral method Isomorphism to a classical system with replicated particles





#### Each calculation is independent The method is thus trivially parallelizable

JM. Soler (UAM), Rafael Ramírez (ICMM)



### van der Waals interactions



### Non-local functional, implemented efficiently in SIESTA (JM Soler, UAM)



Stability of clathrate hydrates Wang, Roman-Perez, Soler, Artacho, Fernandez-Serra, JCP (2011)





### Quantum and van der Waals effects in hydrogen-rich systems: water and clathrate hydrates







• TASK 8.3: "Preparation and Execution of Radiation Damage simulations"

- Simulation of "atomic" collisions.
- Energy loss due to electron heating effects (coupled electron-ion dynamics)

#### Thousands of atoms, and long times, needed in the simulation



### Quasi two-dimensional systems

Lateral graphene-BN heterostructures



#### Moiré patterns of graphene over hex-BN







5 nm



## Ongoing work

- Final refinements to PEXSI method to allow the performance of converged large scale calculations, including molecular dynamics simulations.
- Completion of the upgrade of the I/O subsystem in SIESTA.
- Further work on sparse matrix library to streamline the coding of the O(N) method.



### Collaborations

- Optimization of SIESTA: BSC-CASE.
- Pole-Expansion plus Selected-Inversion method: Lin Lin, Chao Yang (L. Berkeley Lab)
- Quasi-2D graphene-based systems: Miguel Pruneda, Rafael Martínez (CIN2, Barcelona)
- Radiation damage (D. Sánchez-Portal, centro mixto CSIC-UPV (San Sebastián) and M. Pruneda, CIN2)
- Structure of water and quantum effects: M.V. Fernández-Serra, Stony Brook U, R. Ramírez, ICMM.
- Work towards GPU implementation: NVIDIA

